

# Inference Graphs for CNN Interpretation

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#### Motivation for CNN interpretation

The current state –

State-of-the-art results for a variety of computer domains.

The problem –

Reasoning of their decision-making process is lacking.

Our main challenge –

Improving interpretability of the network inference process.





### Our challenges

Can we convert distributed representations into a human-oriented language?





### Our challenges

#### Can we learn a dictionary of visual words and model their interrelationships?









## Generative modeling of MLPs

Trained MLP inference process as a Hidden Markov Model (HMM):

- Single MLP layer distribution: a mixture model of multivariate Gaussians (GMM).
- Connections between layer representations: conditional probability tables between GMM components of adjacent layers.
- Post-Relu activations: rectified Gaussians via additional hidden variables.
- **Optimization:** online Expectation Maximization (EM).





#### Layers Dictionaries for CNNs

- Each spatial location example vector  $x_p^l$  , located at
  - $p = (i, j) \in \{\{1, ..., H^l\} \times \{1, ..., W^l\}\},$  is described as arising from a GMM of  $K^l$  components.
- Example  $x_p^l$  is assigned to cluster  $C_k^l$  iff  $P(h_p^l = k | x_p^l)$  is the highest.
- Each cluster  $C_k^l$  represents a **visual word** (edge, texture, body part etc.), together forming the layer **dictionary**.





#### Layers Dictionaries for CNNs

#### Train a CNN-GMM model:

- 1. Get a pre-trained CNN.
- 2. For every modeled layer l, append to it a GMM layer with the GMM parameters  $\Theta^{l} = \{\pi_{k}^{l}, \mu_{k}^{l}, \Sigma_{k}^{l}\}_{k=1}^{K^{l}}$  as learning weights.
- 3. Train all GMM layers and estimate their parameters independently, using SGD.





#### Graph Node Selection Algorithm

Consider a graph in which visual words  $\{C_k^l\}_{l=1,k=1}^{L,K^l}$  are the nodes, and transition probabilities between visual words of consecutive layers quantify edges.

Given a selected subset of images to be explained  $\Omega = \{I_n\}_{n=1}^{N}$  (e.g., class or a single image), a specific subgraph can have high explanatory value.

How can we find the most explanatory visual words?

#### Node selection algorithm –

iterative algorithm starting from "explaining" the classification decision node, then explaining layers backward, until outputting a subgraph.





#### Graph Node Selection Algorithm

Given an instance of a single visual word  $h_p^l = s$  to "explain", we look for the visual words T in its receptive field R(p) most contributing to its likelihood:

$$\max_{T,|T|=Z} \log P\left(h_p^l = s | h_q^{l'} : q \in R(p), h_q^{l'} \in T\right)$$

Using location independence assumptions, a 't –explains–s' score is derived:

$$S^{l'}(s,t) = \sum_{t=1}^{K^{l'}} \left| \left\{ q: h_q^{l'} = t, q \in R(p) \right\} \right| \log \frac{P\left(h_q^{l'} = t | h_p^{l} = s, q \in R(p)\right)}{P\left(h_q^{l'} = t\right)}$$

the number of times visual word t appears in the receptive field of location p

how likely it is to see word t in the receptive field of s compared to seeing it in general



#### Cluster Similarity Across Layers



increasing similarity between clusters representing the same class.

the clusters stay local and diverse, even at the uppermost layers.



### VGG-16 Image Inference Graph

Ground truth: Pineapple

Network prediction: Swing





## VGG-16 Image Inference Graph



5/196





#### ResNet50 Image Inference Graph

#### Ground truth: Pineapple

Network prediction: Pineapple





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