Accepted Man	nuscript	ELSENTER	589.90-401
Dynamics of disordered type-II Superconductors: peak effect and the I-V curves G. Bel, D.P. Li, B. Rosenstein, V. Vinokur, V. Zhuravlev		PHYSICA Physica Phy	G Superconductivity and its applications
PII: DOI: Reference:	S0921-4534(07)00585-0 10.1016/j.physc.2007.04.169 PHYSC 124129		
To appear in:	Physica C	Available online at	http://www.elsevier.com/locate/physc

Please cite this article as: G. Bel, D.P. Li, B. Rosenstein, V. Vinokur, V. Zhuravlev, Dynamics of disordered type-II Superconductors: peak effect and the I-V curves, *Physica C*(2007), doi: 10.1016/j.physc.2007.04.169

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting proof before it is published in its final form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

# ACCEPTED MANUSCRIPT

Physica C



PHYSICA

# Dynamics of disordered type-II Superconductors: peak effect and the I-V curves

G. Bel<sup>a</sup>, D.P. Li<sup>b</sup>, B. Rosenstein<sup>c</sup>, V. Vinokur<sup>d</sup>, and V. Zhuravlev<sup>c</sup>

<sup>a</sup> University of California, Department of Chemistry, Santa Barbara, CA, US, <sup>b</sup> Beijing University, School of Physics, Beijing, China, <sup>c</sup> National Chiao Tung University, Department of Electrophysics, Hsinchu, Taiwan, ROC, <sup>d</sup> Argonne National Lab, Material Science Division, Argonne,, USA

Elsevier use only: Received date here; revised date here; accepted date here

#### Abstract

We quantitatively describe the competition between the thermal fluctuations and disorder by the Ginzburg - Landau approach using both the replica method in statics and the dynamical Martin-Siggia-Rose approach which allows generalization beyond linear response. The two methods are consistent in static, while the dynamical method allows calculation of the critical current as function of magnetic field and temperature. The surface in the J-B-T space defined by this function separates between a dissipative moving vortex matter regime and vortex glass. The non-Ohmic I-V curve is obtained.

Keywords: Type II superconductor, Glass transition, Quenched disorder

# 1. Introduction

Calculation of the thermodynamic, magnetic and transport characteristics of the vortex matter in type II superconductors subject to both the quenched disorder and thermal fluctuations is a long standing problem. The main difficulty is to account for the "glassy" properties of the vortex matter. The vortex matter can be treated in various regions of the external parameters space (including magnetic field *H*, temperature *T*, and electric field *E* in dynamics) either in London approximation (far from  $H_{c2}$ ), Ginzburg – Landau approximation (far from  $H_{c1}$ ) or using more phenomenological models of vortex lines. In this paper we use the time dependent GL equation and the dynamical Martin-Siggia-Rose approach. The obtained results are compared with that derived in the replica method.

# 2. The irreversibility line and peak effect critical current

We obtain the following line separating the vortex liquid from the vortex glass:

$$a_T^g = (2r)^{2/3} (3 - 2/r) , \qquad (1)$$

where 
$$a_T = -\frac{2^{5/3}}{(2Gi)^{1/3}(bt)^{2/3}}(1-t-b)$$
 and  $r = \frac{a_h^2}{\pi\sqrt{2Git}}n$ 

are determined by disorder parameter, *n*, proportional to density of the pinning centers, Ginzburg number, *Gi*, and by dimensionless parameters  $t=T/T_c$ ,  $b=H/H_{c2}(0)$ .



Fig 1. *H-T* phase diagram with  $H_{c2}(T)$  line (upper straight line), glass line, Eq. (1), (middle curve), and melting line (down curve). Experimental values (points) for glass transition are taken from [1].

# ACCEPTED MANUSCRIPT



Fig 2. Magnetic field dependence of the critical current in the vortex glass phase (solid line) and in the vortex crystalline phase (dash line) in comparison with experimental data [4] (points).

Very similar line is obtained in the crystalline phase. The line is fitted to the experiment [1] on NbSe<sub>2</sub> in Fig.1. The melting line calculated in [2] in this case is below the irreversibility line unlike in BSCCO where they intersect [3]. This leads to the peak effect in magnetisation curve M(H), shown in Fig. 2.

The critical current,

$$I_{c} = \frac{(bt)^{2/3} (Gi/r)^{1/3}}{2^{8/3} (2\pi)^{2}} \left[ 1 - t - b + (2Gi)^{1/3} (rbt)^{2/3} (3 - \frac{2}{r}) \right]$$

is defined as a current at which the glass is depinned and becomes a flow, neglecting exponentially small creep. It is found in a good agreement with transport data of [4] (see also [5]).

### 3. The I-V curves

Contributions from the LLL and via first Landau level are:

$$j_{LLL} = \frac{R_0}{32\pi} \left( 4t^2 Gi / b \right)^{1/3} E$$
(2)

$$j_d = 2^{1/3} \sqrt{\left(\sqrt{2} - 1\right)/3\pi t} \left(bt\right)^{2/3} r^{1/6} \left(2Gi\right)^{5/6}$$
(3)

where dimensionless units for both, electrical current and field, have been used and the response function  $R_0$  is obtained as a solution of the equation:  $-4(1-r)R_0^3 - a_T R_0^2 + 1 = 0$ . The first contribution is dissipative and consistent with Bardeen – Stephen, while the second contains the persistent current. They are similar to that in [5,6].

Physica C



Fig 3. *E-I* -curve for parameters above (1),below (3,4), and on the glass transition line (2).

#### Summary

We present a quantitative theory of the vortex liquid to vortex glass transition with both thermal fluctuations and random quenched disorder effects and compare it to experiment on NbSe<sub>2</sub>.

It is shown that the static flux line lattice in type II superconductors undergoes a transition into three disordered phases: vortex liquid (not pinned), homogeneous vortex glass (pinned) and crystalline Bragg glass (pinned) due to both thermal fluctuations and random quenched disorder. The location of the glass transition line is determined and compared to experiments. The line is clearly different from both the melting line and the second peak line describing the translational and rotational symmetry breaking at high and low temperatures respectively.

### Acknowledgments

This research is supported by NSC of R.O.C., NSC#932112M009024 (B.R.,V.Z.).

# References

[1] S.S. Banerjee, et al., Physica C 355, 39 (01).

[2] D.P. Li, B. Rosenstein, Phys. Rev. Lett. 90, 167004

- (03); Phys.Rev. B 70, 144521 (04).
- [3] H. Beidenkopf et al, Phys. Rev. Lett. 95, 257004 (05).
- [4] N.Kokubo et al., Phys. Rev. Lett. B 95, 177005 (05)

[5] O. Dogru et al, Phys. Rev. Lett. **90**, 167004; Y. Paltiel et al, Phys. Rev. Lett. **85**, 3712 (00).

[6] A.D. Thakur et al, Phys. Rev B **72**, 134524 (05); A. Pautrat et al . Rev B **71**, 064517 (05).